

SCIENTIFIC AMERICAN



CELLULAR AUTOMATON

ONE DOLLAR

February 1971

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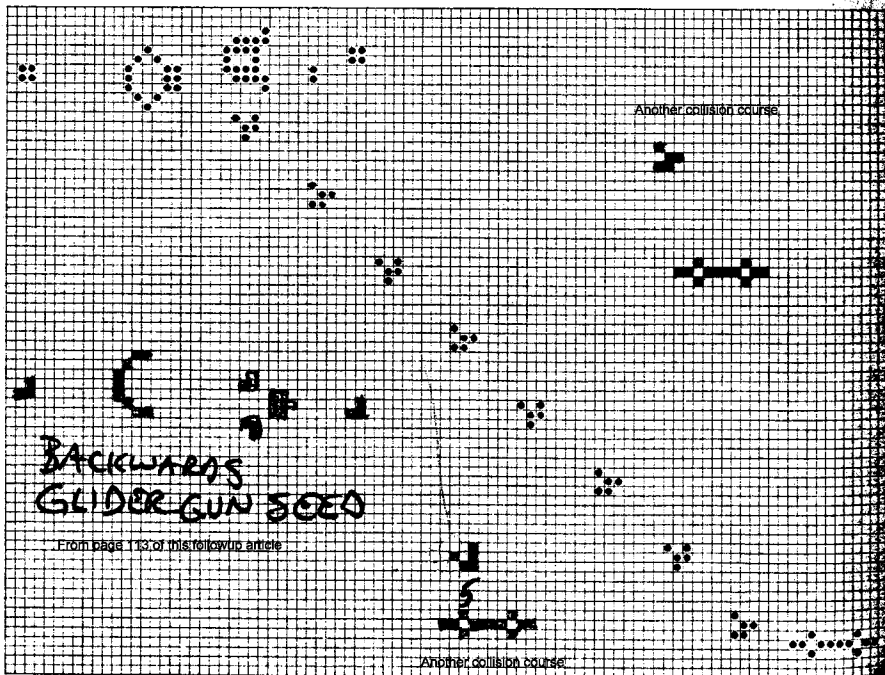
Slotnick, page 76). The cover of this issue of SCIENTIFIC AMERICAN shows a simple procedure, devised by Smith, by which a finite one-dimensional cellular space employs parallel computation for recognizing palindromic symmetry. Each cell has many possible states, the number depending on the number of different symbols in the palindrome, and a cell's neighborhood is the two cells on each side.

On the cover, which Smith designed, he symbolizes the palindrome TOO HOT TO HOOT with four states of cells in the top row. *T*, *O* and *H* are represented by blue, red and yellow respectively, and black marks the palindrome's two ends. The white cells in the other rows are in the quiescent state. The horizontal rows below the top row are successive generations of the top configuration when certain transition rules are followed in discrete time steps. In other words, the picture is a space-time diagram of a single row, each successive row indicating the next generation.

In the first transition each color travels one cell to the left and one cell to the right, except for the end colors, which are blocked by black; black moves inward at each step. Each cell on which two colors land acquires a new state, symbolized by a cell divided into four triangles. The left triangle has the color that was previously on the left, the right triangle has the color previously on the right. The result of this first move is shown in the second row. When an adjacent pair of cells forms a tilted square in the center that is a solid color, it indicates a "collision" of like colors and is symbolized by black dots in the two white triangles of the left cell. Dots remain in that cell for all subsequent generations unless a collision of unlike colors occurs to the immediate right of the dotted cell, in which case the dots are erased. When collisions of *unlike* colors occur, the left cell of the pair remains undotted for all subsequent generations even though like colors may later collide on its right.

At each move the colors continue to travel one cell left or right (the direction in which the colored triangles point) and all rules apply. If the palindrome has n letters, with n even as in this example (the scheme is modified slightly if n is odd), it is easy to see that after $n/2$ moves only two adjacent nonquiescent cells remain. If the left cell of this pair is dotted, the automaton has recognized the initial row as being palindromic. Down the diagram's center you see the colliding pairs of like colors in the same order as they appear on the palindrome from the center to each end. As soon as recognition occurs the left cell of the last pair is erased and the right cell is altered to an "accept" state, here symbolized by nested squares. An undotted left cell would signal a nonpalindrome, in which case the left cell would become blank and the right cell would go into a "reject" state.

A Turing machine, which computes serially, requires in general n^2 steps to recognize a palindrome of length n . Al-

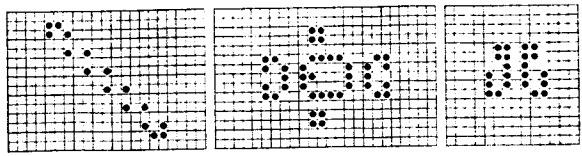


Pentadecathlon (bottom right) "eats" gliders (color) fired by the gun

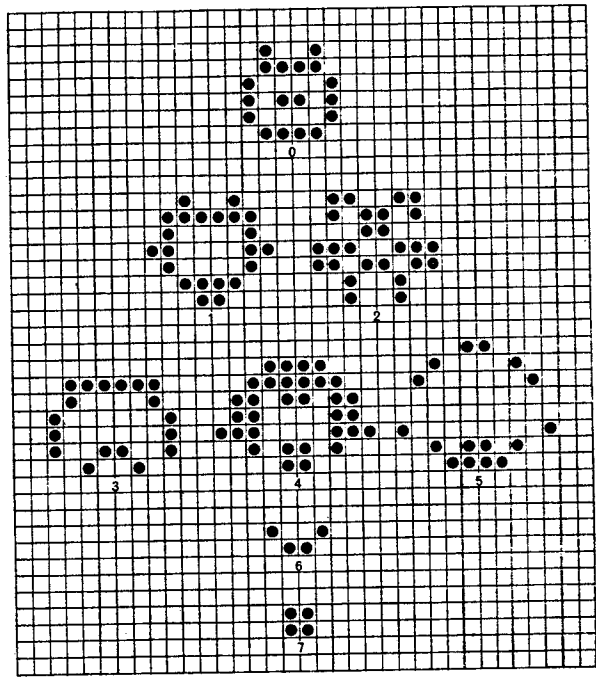
though recognition occurs here at step 2, the accept state is shown moving in subsequent generations to the right to symbolize the cell-by-cell transmission of the acceptance to an output boundary of the cellular space. Of course it is easy to construct more efficient palindrome-recognizing devices with actual electronic hardware, but the point here is to do so with a highly abstract, one-dimensional cellular space in which information can pass only from a cell to adjacent cells and not even the center of the initial series of symbols is known at the outset. As Smith puts it anthropomorphically, after the first step each of the three dotted cells thinks it is at the center of a palindrome. The dotted cells at each end are disillusioned on the next move because of the collision of unlike colors at their right. Not until generation $n/2$ does the dotted cell at the center know it actually is at the center.

Now for some startling new results concerning Conway's game. Conway was fully aware of earlier games and it was with them in mind that he selected his recursive rules with great care to avoid two extremes: too many patterns that grow quickly without limit and too many that fade quickly. By striking a delicate balance he designed a game of surprising unpredictability and one that produced such remarkable figures as oscillators and moving spaceships. He conjectured that no finite population could grow (in number of members) without limit, and he offered \$50 for the first proof or disproof. The prize was won in November by a group in the Artificial Intelligence Project at M.I.T. consisting of (in alphabetical order) Robert April, Michael Beeler, R. William Gosper, Jr., Richard Howell, Rich Schroepel and Michael Speciner. Using a program devised by Speciner for displaying moves on an oscilloscope, Gosper made a truly astounding discovery: he found a glider gun! The configuration in the lower illustration on page 113 grows into such a gun, firing its first glider on move 40. The gun is an oscillator of period 30 that ejects a new glider every 30 moves. Since each glider adds five more counters to the field, the population obviously grows without limit.

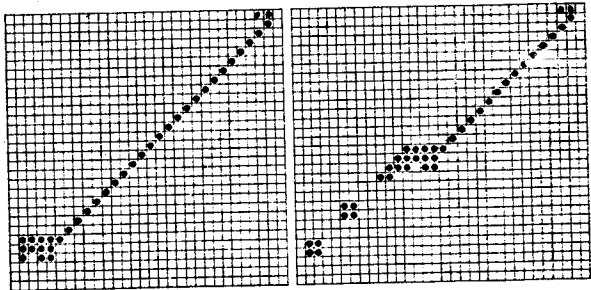
The glider gun led the M.I.T. group to many other amazing discoveries. A series of printouts (supplied by Robert T. Wainwright of Yorktown Heights, N.Y.) shows how 13 gliders crash to form a glider gun [see illustration on page 117]. The last five printouts show the gun in full action. The group also found a way to position a pentadecathlon [see



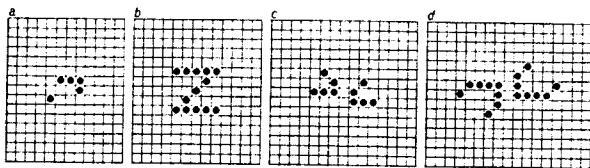
Barber pole (left), Hertz oscillator (middle) and tumbler (right)



The Cheshire cat (0) fades to a grin (6) and disappears, leaving a pac print (7)



The harvester, shown at generations 0 (left) and 10 (right)



Two spanners of gliders and two collision courses

illustration on page 114), an oscillator of period 15, so that it "eats" every glider that strikes it. A pentadecathlon can also reflect a glider 180 degrees, making it possible for two pentadecathlons to shuttle a glider back and forth forever. Streams of intersecting gliders produce fantastic results. Strange patterns can be created that in turn emit gliders. Sometimes collision configurations grow until they ingest all guns. In other cases the collision mass destroys one or more guns by shooting back. The group's latest burst of virtuosity is a way of placing guns so that the intersecting streams of gliders build a factory that assembles and fires a lightweight spaceship every 300 moves.

The existence of glider guns raises the exciting possibility that Conway's game will allow the simulation of a Turing machine, a universal calculator capable in principle of doing anything the most powerful computer can do. The trick would be to use gliders as unit pulses for storing and transmitting information and performing the required logic operations that are handled in actual computers by their circuitry. If Conway's game allows a universal calculator, the next question will be whether it allows a universal constructor, from which nontrivial self-replication would follow. So far this has not been achieved with a two-state space and Conway's neighbor-

hood, although it has been proved impossible with two states and the von Neumann neighborhood.

The M.I.T. group found many new oscillators [see top illustration on preceding page]. One of them, the barber pole, can be stretched to any length and is a flip-flop, with each state a mirror image of the other. Another, which they rediscovered, is a pattern Conway's group had found earlier and called a Hertz oscillator. Every four moves the colored "bit" switches from one side of the central frame to the other, making it an oscillator of period 8. The tumbler, which was found by George D. Collins, Jr., of McLean, Va., turns upside down every seven moves.

The Cheshire cat [see middle illustration on preceding page] was discovered by C. R. Tompkins of Corona, Calif. On the sixth move the face vanishes, leaving only a grin; the grin fades on the next move and only a permanent paw print (block) remains. The harvester was constructed by David W. Poyner of Basildon in England. It plows up an infinite diagonal at the speed of light, oscillating with period 4 and ejecting stable packages along the way [see bottom illustration on preceding page]. "Unfortunately," writes Poyner, "I have been unable to develop a propagator that will sow as fast as the harvester will reap."

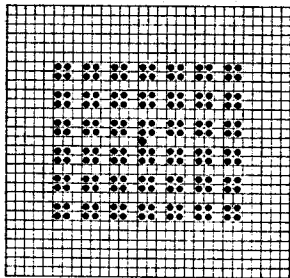
Wainwright has made a number of intriguing investigations. He filled a 120-by-120 square field with 4,800 randomly placed bits (a density of one-third) and tracked their history for 450 generations, by which time the density of this primordial soup, as Wainwright calls it, had thinned steadily to one-sixth. Whether it would eventually vanish or, as Wainwright says, percolate at a constant minimum density is anybody's guess. At any rate, during the 450 generations 42 short-lived gliders were formed. Wainwright found 14 different patterns that became glider states on the next move. The pattern that produced the greatest number of gliders (14 in all) is shown ["a" in illustration above]. A Z-pattern found by Collins and by Jeffrey Lund of

Pewaukee, Wis., after 12 moves becomes two gliders that sail off in opposite directions [b]. Wainwright and others set two gliders on a collision course that causes all bits to vanish on the fourth move [c]. Wallace W. Wagner of Anaheim, Calif., found a collision course for two lightweight spaceships that also ends (on the seventh move) in total blankness [d].

Wainwright has experimented with various infinite fields of regular stable patterns, which he calls agar-rich culture mediums. When, for instance, a single "virus," or bit, is placed in the agar of blocks shown in the illustration at bottom left so that it touches the corners of four blocks, the agar eliminates the virus and repairs itself in two moves. If, however, the alien bit is positioned as shown (or at any of the seven other symmetrically equivalent spots), it initiates an inexorable disintegration of the pattern. The portion eaten away contains active debris that has overall bilateral symmetry along one axis and a roughly oval border that expands, probably forever, in the four compass directions at the speed of light.

The most immediate practical application of automata theory, Banks believes, is likely to be in the design of circuits capable of self-repair or the wiring of any specified type of new circuit. No one can say how significant the theory may eventually become for the physical and biological sciences. It may have important bearings on cell growth in embryos, the replication of DNA molecules, the operation of nerve nets, genetic changes in evolving populations and so on. Analogies with life processes are impossible to resist. If a primordial broth of amino acids is large enough, and there is sufficient time, self-replicating moving automata may result from complex transition rules built into the structure of matter and the laws of nature. There is even the possibility that space-time itself is granular, composed of discrete units, and that the universe, as Fredkin and others have suggested, is a cellular automaton run by an enormous computer. If so, what we call motion may be only simulated motion. A moving spaceship, on the ultimate microlevel, may be essentially the same as one of Conway's spaceships, appearing to move on the macrolevel whereas actually there is only an alteration of states of basic space-time cells in obedience to transition rules that have not yet been discovered.

To the corrections given last month for the original discussion of Conway's game the following should be added. At



Pattern doomed by a virus (color)

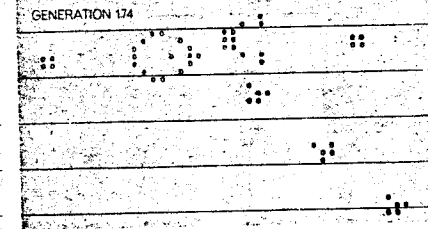
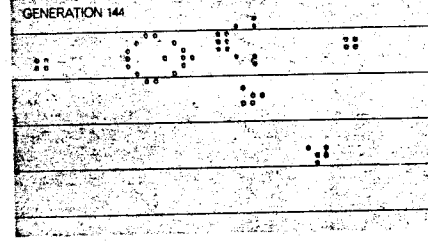
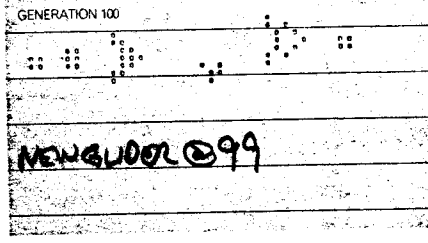
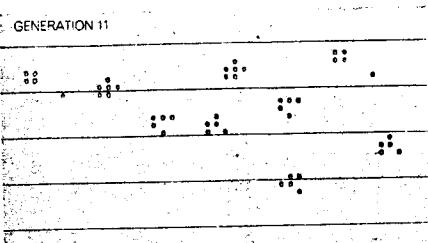
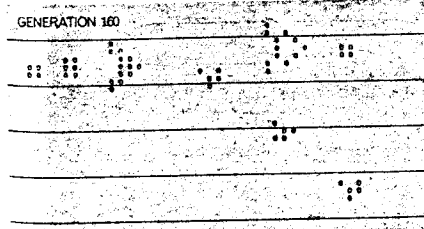
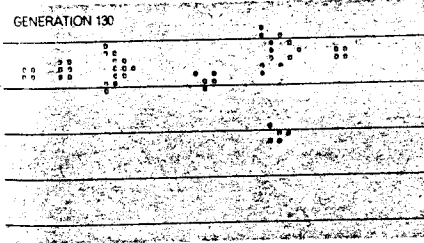
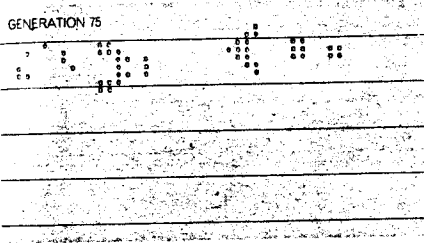
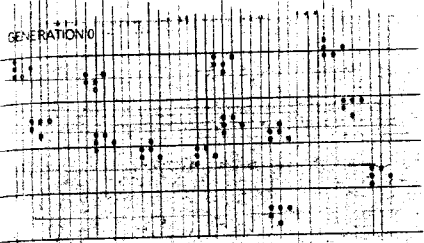
original row of eight adjacent coun-
 erparts as four blocks and four bee-
 es, and the 5-5 row ends as four
 cks and two blinkers. In November's
 stration of a large spaceship escorted
 two smaller ones, the top ship should
 be separated by three cells from
 middle one. Readers too numerous to
 mention have confirmed all three correc-
 tions.

The number puzzles posed last month
 by Dr. Matrix have the following an-
 swers. In addition to 9,240, the only
 other number smaller than 10,000 that
 has 63 proper divisors (including 1 but
 not the number itself) is 7,560. No other
 number of four or fewer digits has this
 many proper divisors. Here is the only
 way to arrange two three-digit square
 numbers in a two-by-three matrix so that

each column, read from the top down, is
 a two-digit square:

841
 196.

A newsletter, *The Soma Addict*, is
 now available at no charge on request
 from Parker Brothers, P.O. Box 900,
 Salem, Mass. 01970.



How 13 gliders (color) crash to form a glider gun (generation 75) that oscillates with a period of 30, firing a glider in each cycle